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**SUBJECT CODE NO:- B-2122**  
**FACULTY OF SCIENCE & TECHNOLOGY**  
**B.Sc. T.Y. (Sem-VI)**  
**Examination November/December- 2022**  
**Mathematics**  
**Mathematical Statistics-II – MAT -603**

[Time: 1:30 Hours]

[Max. Marks:50]

Please check whether you have got the right question paper.

- N.B
- 1) All questions are compulsory.
  - 2) Figures to the right indicate full marks.
- Q.1 A) Attempt any one: 08
- a) if X and Y are random variables then prove that:  
 $E(X+y)=E(x) + E(y)$ ,  
 provided that both the expectations exist
  - b) if X is a random variables, then prove that  
 $v(ax + b) = a^2 v(x)$ ,  
 Where a and b constants.  
 Also prove that variance is independent of change of origin and scale.
- Q.1 B) Attempt any one: - 07
- c) Two unbiased dice are thrown find the expected values of the sum of numbers of points on them.
  - d) If x is a Poisson variate such that  
 $P(x = 2) = gp(x = 4) + 90 P(x = 6)$   
 Find (i)  $\lambda$  ii) The Mean.
- Q.2 A) Attempt any one: 08
- a) Find first four central moments of a binomial distribution by using moment generation function.
  - b) Find the moment generating function of exponential distribution.

B) Attempt any one:

07

- Q.2 c) Ten coins are thrown simultaneously. Find the probability of getting at least seven heads.  
 d) If  $x$  and  $y$  are independent Poisson variates such that  $P(X=1)=P(x=2)$  and  $P(y=2)=P(y=3)$  find the variance of  $x-2y$

Q.3 A) Attempt any one:

05

- a) Find the median of normal distribution.  
 b) Prove that correlation coefficient is independent of change of origin and scale.

Q.3 B) Attempt any one:

05

- a) Determine the binomial distribution for which the mean is 4 and variance 3 and find its mode..  
 b) If  $x$  has a Uniform distribution in  $[0,1]$  find the distribution (p.d.f) of  $-2\log x$ . Identify the distribution also.

Q.4 Choose the correct alternative.

10

- i. If  $x$  and  $y$  are independent then  $\text{cov}(x,y)=$ -----  
 a) 1    b) 0    c) -1    d) 2
- ii. The mean of Poisson variate is -----its variance.  
 a) Greater than    b) less than    c) equal to    d) twice
- iii. The moment generating function of gamma distribution is -----  
 a)  $(1+t)^\lambda$     b)  $(1-t)^\lambda$     c)  $(1-t)^{-\lambda}$     d)  $(1+t)^{-\lambda}$
- iv. The mean and median of normal distribution are -----  
 a) The same    b) Not Same    c) Mean < Median    d) Mean > median
- v. The variance of Bernoulli distribution is -----  
 a)  $p$     b)  $pq$     c)  $q$     d)  $p-q$